In situ electron holography of the dynamic magnetic field emanating from a hard-disk drive writer

Joshua F. Einsle¹, Christophe Gatel²(✉), Aurélien Masseboeuf², Robin Cours², Muhammad A. Bashir⁴, Mark Gubbins⁴, Robert M. Bowman¹, Etienne Snoeck²

Nano Res., Just Accepted Manuscript • DOI: 10.1007/s12274-014-0610-0
http://www.thenanoresearch.com on October 16 2014
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This article reports on the complete *in situ* quantitative mapping of the magnetic field generated by a functioning write pole in operation using electron holography.

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ABSTRACT

The proliferation of mobile devices in society accessing data via the ‘cloud’ is imposing a dramatic increase in the amount of information to be stored on hard disk drives (HDD) used in servers. Forecasts are that areal densities will need to increase by as much as 35% compound per annum and by 2020 cloud storage capacity will be around 7 zettabytes corresponding to areal densities of 2 Tb/in². This requires increased performance from the magnetic pole of the electromagnetic writer in the read/write head in the HDD. Current state-of-art writing is undertaken by morphologically complex magnetic pole of sub 100 nm dimensions, in an environment of engineered magnetic shields and it needs to deliver strong directional magnetic field to areas on the recording media around 50 nm x 13 nm. This points to the need for a method to perform direct quantitative measurements of the magnetic field generated by the write pole at the nanometer scale. Here we report on the complete in situ quantitative mapping of the magnetic field generated by a functioning write pole in operation using electron holography. Opportunistically, it points the way towards a new nanoscale magnetic field source to further develop in situ Transmission Electron Microscopy.
1. Introduction

The read/write head is the small active part of the slider component located at the end of the actuator arm inside a HDD. A schematic drawing of a slider is shown in Fig. 1a. In Fig. 1b is a SEM image of the read/write parts that face the media with a zoom of the write pole region. The yellow arrows illustrate the direction of travel of the media beneath the write pole. The writing/erasing magnetic field is generated by the current flowing in the coils intended to behave linearly with the applied current without hysteresis when reversing the current to allow for the fast, accurate writing and erasing of data [1] (a cross section of the read/write element is presented in Fig. S1 and S2 in the Electronic Supplementary Material (ESM) on which the yoke and return poles of the writer electromagnet and the drive coils are identified). To precisely tailor the profile of emanating magnetic field, the current carrying coils and bulk magnetic material of the writer are shielded from the disk media. This also insures that the magnetic environment experienced by the media is dominated by the write pole and not from other surfaces of this three dimensional electromagnetic device. These shields are composed of soft magnetic materials to intensify the magnetic field gradients coming out of the write pole and are shown in the zoom Fig. 1b.

Current understanding about the behaviour, shape and strength of the magnetic field generated by this nanoscale electromagnet arises from indirect methods. Either the size and shape of the written magnetic bits are measured on the magnetic media [2] or numerical simulations are performed to visualize the fields emanating from the pole. With continued downscaling of the write pole to critical dimensions numerical approaches will become essential but computationally complex. Additionally, the development of new technologies like Heat Assisted Magnetic Recording (HAMR) [3,4] which combines an optical field to reduce the media coercivity with the writing/erasing magnetic field will make magnetic write tests even more difficult. A direct approach for the visualization and quantification of the magnetic field produced by a write pole would be of significant technological benefit for the characterization of HDD read/write heads performance. In this study, we have developed such a tool, by combining the powerful TEM technique of off-axis electron holography (EH) with in situ electrical biasing to actively vary the magnetic field.
field produced by a fully operational HDD write pole. Electron Holography (EH) is an efficient interferometric TEM method enabling the quantitative mapping of local electrostatic and magnetic fields with a resolution of few nanometres over a field of view as large as few microns [5-9]. For this particular study, we have developed a new set-up allowing for the first time to quantitatively map the magnetic fields generated by the writer as a function of applied electrical currents up to ±60 mA. The resulting quantified magnetic field maps demonstrate the key features required in magnetic recording, namely a highly directional magnetic field with low angular spread.

Further, while we are able to tune the applied current in series of steady state steps, this dynamic fluxing of the magnetic field paves way for two innovative applications in EH. The writer and its wiring circuitry are designed to operate to GHz frequencies; it therefore opens up the potential for the acquisition of quantitative information of the magnetic induction generated by the writer as a function of the applied current frequency. Then, of more general interest, it points to a new development of new in situ EH TEM experiments whereby a nanoscale magnetic field source can be incorporated into sample stage assemblies for in situ magnetic experiments of wider interest.

2. Experimental

The write pole has been an extensively studied device due to its importance in the operation of HDDs. Along with other techniques, EH has been used to study thin section lamellae of the write pole [7,8] and demonstrates how magnetic domains form under various externally applied magnetic fields. These basic experiments do not, however, give information about the generation of a magnetic field by the write pole itself in operating conditions when electric current is sent into the coils. Recently, in situ EH approaches have been attempted to characterize the write pole device [9]. While Goto et al. demonstrate that a field can be imaged in situ they did not fully isolate and characterize the magnetic field of the write pole in operational conditions. Presenting only partial magnetic information with the writer still imbedded in the shield material, the magnetic signal resulting of the current flowing in the coils cannot be separate from the one due to the shields neither from additional artefacts originating from electrostatic potential. We have developed a novel strategy that allows imaging an operational write pole in situ in a TEM in normal conditions, to obtain the complete local hysteresis loop on each point of a large area and quantitatively separate the magnetic signals originating solely from the write pole and those of the shield material, while dynamically changing the applied current through the write coils.

As outlined the difficulty in developing a method for directly imaging the write pole's magnetic fields lies in keeping the necessary electrical circuitry undamaged to drive the writer, while making it fit in a TEM stage. In this work, we achieve this through reducing the overall size of a HDD slider from 1.2 mm down to 30 μm by mechanically polishing while keeping intact the electrical contacts pads and coils used by the device. An additional issue is to provide a scheme to locate the plane in which the write pole resides, because in this EH experiment the electron beam passes adjacent to the face of the write pole. To do so, Focussed Ion Beam Induced Deposition was used to grow a pair of fiducial carbon pillars on each side of the write pole prior to TEM investigation. The thinned device is then wire bonded to an in situ electrical biasing holder and transferred to the microscope (sample preparation details are given in SI).

The in situ TEM experiment was performed in Lorentz mode on a Cs-corrected Tecnai F20 microscope operating at 200kV. A Möllensted biprism, positioned parallel to the surface of the slider at a distance of about 600 nm, is used to create the interference pattern between part of the
electron beam interacting with the generated magnetic induction field in front of the write pole and part of the beam that passes far from it through an almost field-free region, so-called “reference beam” (a low magnification image of the whole area is given in the SI). The analysis of the interference pattern (i.e. the electron hologram) allows extraction of the phase shift between the reference beam and the one that has interacted with the magnetic induction.

In our experiment, the electron phase shift \( r \) is only related to the magnetic induction through the Aharanov-Bohm relation [10,13]:

\[
\phi(r) = - \frac{e}{\hbar} \int B_\perp(r,z) \, dr \, dz
\]

where \( r = (x,y) \) represents the position vector in the plane perpendicular to the electron path (x and y directions), \( e \) the elementary charge, \( B_\perp \) the component of the magnetic induction in the plane perpendicular to \( r \) and to the beam direction \( z \). The measured phase shift corresponds to a projection and an integration of all in-plane magnetic field contributions along the electron path. Numerical simulation are generally unavoidable to take into account the two dimensional projection of a three dimensional field.

3. Results and discussion

3.1 Magnetic phase shift as function of current

Applying a current on the device generates a magnetic field that can be directly visualized studying the phase image calculated in-line from the hologram [14]. After determining the precise location of the write pole and adjusting carefully the orientation of its exposed surface parallel to the electron beam, we fully characterized the generated magnetic induction by collecting two series of 44 holograms. A first sequence was acquired with the applied current varying from -60 mA to +60 mA, and a second series reverses this sequence by running the current from +60 mA to -60 mA to effectively perform a hysteresis loop measurements. Phase shift images obtained with currents of -60 mA, -10 mA, 0 mA, 10 mA, 60 mA are reported in the left column of Fig. 2. The projected magnetic field is parallel to the isophase lines. Considering that \( B_\perp = (B_x, B_y) \), the x and y components of the magnetic induction integrated over the beam path can then be extracted calculating respectively the \( y \) and \( x \) derivatives of the phase shift image (after unwrapping to remove the phase jumps) following the equations:

\[
\int B_x(r) \, dz = -\frac{\hbar}{e} \frac{dy}{dx} \phi(r)
\]

\[
\int B_y(r) \, dz = \frac{\hbar}{e} \frac{dx}{dy} \phi(r)
\]

\[ \int B_x(r) \, dz \] and \[ \int B_y(r) \, dz \] are mapped using Eq. 2a and 2b and reported in the two columns on the right side of Fig. 2 for the five corresponding currents. The phase images and magnetic field components are symmetric with respect to the “x” axis for applied current of opposite sign. For 0 mA applied current the magnetic flux is only between the shields located on each side of the pole indicating that the integrated \( B_x \) component of the magnetic induction is zero for the direction perpendicular to the write pole.

Beside these two dimensional maps of the magnetic induction generated by the write pole in operation, the EH experiment allows for the quantitative determination of the induction field at any point of the studied area and for each value of the applied D.C. current. It then permits extraction of local hysteresis loops of the two components of the magnetic induction. As an illustration, we extracted four hysteresis loops of the \( B_x \) and \( B_y \) components averaged over a \( (5 \times 5) \, \text{nm}^2 \) region at four different
Figure 2 Left column: Experimental phase image of the magnetic flux recorded in front of the write pole for an applied current of +60 mA, +10 mA, 0 mA, -10 mA and -60 mA. Middle column: Corresponding B$_x$ components map integrated over the beam path. Right column: Corresponding B$_y$ components map integrated over the beam path. The white rectangle on the middle left side of each image is the write pole location.

Positions in front of the device (noted 1, 2, 3, 4 in the first B$_x$ and B$_y$ images of Fig. 2) for current varying from +60 mA to -60 mA then from -60 mA to +60 mA. These local hysteresis loops are reported in Figs. 3a and 3b for B$_x$ and B$_y$ respectively. The two B$_x$ hysteresis loops in Fig. 3a evidence that the magnetic saturation is reached for an applied current of about 25 mA. They also indicate the absence of remnant and coercive fields that both are expected for a HDD read/write device. This results also evidences the induction field reduction when moving away from the central part of the pole i.e. when moving from position (1) located at 5 nm in front of pole to position (2) displaced by 50 nm both in x and y directions (This magnetic field decrease is also evidenced on Fig. S5).

Figure 3 a) Hysteresis loops of the B$_x$ component extracted from Fig. 2 (middle column) at position (1) and (2). b) Hysteresis loops of the B$_y$ component extracted from Fig. 2 (right column) at position (3) and (4).

The two B$_y$ hysteresis loops reported in Fig. 3b for two symmetrical positions (3) and (4) on each side of the pole (at position $x = 20$ nm and $y = +/-100$ nm) show that the magnetic induction remains symmetric with respect to the write pole. In addition, these B$_y$ hysteresis loops indicate the appearance of a constant magnetic field for zero applied current. This magnetic field is due to the lateral magnetic shields adjacent to the write pole.
The total magnetic induction in front of the write pole is therefore the superimposition of the constant magnetic induction created by the shields and the one generated by the current sent into the writer coils. Changing the polarity of the applied current results in reversing the direction of the induced magnetic field while the shield magnetic induction remains constant. Therefore, the half-sum of two phase-images obtained with reversal current gives the magnetic contribution of the shields while their half difference results in the phase contribution of the writer only. Fig. 4 illustrates the results of these calculations. The images on the top show the magnetic induction created by the writer only for applied currents of 0 mA, +10 mA and +60 mA while the ones at the bottom of the image are the magnetic induction of the shield. The later remains constant and indicates that the shield produces an almost flat and constant magnetic field running between the shields from one side of the write pole to the other. The gradient of the shield induction is perpendicular to the write pole one and much lower.

Figure 4 Upper row: Experimental images of the magnetic flux generated by the write pole for applied currents of 0 mA, +10 mA and +60 mA. Bottom row: Experimental images of the magnetic flux due to the shield which remains constant.

3.2 Micromagnetic Simulations

Such quantitative measurements of the magnetic induction should be confirmed by numerical simulation to ensure that the region where the reference beam has been selected is indeed field free, or contains a negligible field, and does not create artefacts in the final phase image. We use the finite element package Magpar [15] to simulate the entire write pole system using the dimensions of the write pole extracted from SEM images. The standard bulk values of the magnetic constants of the various materials comprising the write pole system are used (writer, shields, etc.). We ensure that the device model and its materials are saturated by the application of an initial current of +40 mA before extracting steady state information. We then generate the magnetic flux spreading in a three dimensional (1 μm, 1.5 μm, 0.8 μm) region in front of the whole device for an applied current of +40 mA (an image of the simulation box is reported in SI Fig. S3 in the ESM).

The resulting magnetic induction flux is used to calculate the phase shift of the electron beam passing across the box. The resulting phase image is reported in Fig. 5a. We then calculated the difference between the simulated phase of the electron beam that has passed within a 500 nm wide region close to the write pole (« object wave area » in Fig. 5a) and the simulated phase of the electron beam that has passed in 500 nm wide region which is not perfectly field free located 500 nm far from it (« reference wave area » in Fig. 5a).

The resulting phase image is reported in Fig. 5b and presents a very good agreement with the experimental one at the same injected current (Fig. 5c). We can note that the modification of the simulated phase due to the weak field in the reference wave area is negligible. A more quantitative comparison can be achieved drawing the simulated (including or nit the reference wave contribution) and experimental induction profiles from the \( B_x \) component at 40 mA (Fig. 6a and 6b) along two directions: one along the “x” direction at position \( y = 0 \) (Fig. 6c), the other along the “y”
direction at position $x = 5$ nm from the writer surface corresponding to the position of the media in operation (Fig. 6d). The simulated profiles fit very well with the experimental ones and confirm the negligible effect arising from the remaining field of the reference area. This result supports both the model we use for the device and the EH procedure. It also confirms that the magnetic induction generated by the write pole is as expected when saturating it, for the materials and geometrical considerations.

**Figure 5**

a) Simulated phase of the electron beam after its interaction with the device magnetic induction over a 500 nm x 1 µm box and projected along the beam path. The biprism is located in the middle of the image and creates interference between the regions 1 and 2 of the electron beam passing on each side of it. The simulation has been realized for an applied current of +40 mA.

b) Simulated phase image resulting on the difference of the phases in region 1 and 2 taking into account the influence of the remaining magnetic induction in the reference beam. The modification arising from the remaining field of the reference area is negligible.

c) Experimental phase image at +40 mA. We can note the very nice agreement with the simulation image in b).

**Figure 6**

a) Experimental image of the $B_x$ component of the magnetic induction for a +40 mA applied current.

b) Simulated image of the $B_x$ component of the magnetic induction for a +40 mA applied current.

c) Experimental (black) profile of the $B_x$ component extracted along the “x” direction at position $y = 0$ (horizontal blue arrow on a)). Simulated profiles in red (without reference area correction) and green (with correction).

d) Experimental (black) profile of the $B_x$ component extracted along the “y” direction at position $x = 5$ nm from the writer surface (vertical blue arrow on a)). Simulated profiles in red (without reference area correction) and green (with correction).
3.3 Magnetic induction mapping

We have shown that EH allows the quantitative mapping of the magnetic induction in front of the device and therefore is appropriate to analyse its capability to focus the flux to a recording media. In addition, the write pole contribution can be perfectly isolated. These in situ EH experiments allows building quantitative 3D data cubes $B_x(x, y, I)$ and $B_y(x, y, I)$ of the local magnetic induction components relevant to characterize the magnetic field generated by the write pole only at various $(x, y)$ positions in front of it (Fig. 7a). The component of the hysteresis loop perpendicular to the device, $B_x$, is of particular interest as it is the part of the induction that writes magnetic bits on the media. A clear visualization of $B_x$ can be obtained plotting a series of $B_x(I)$ hysteresis loops extracted from the data cube $B_x(x, y, I)$ at position $y = 0$, in front of the write pole piece (noted (1) on the Fig. 7a), and for increasing distance from it (i.e. as function of “$x$”). This surface plot is reported in Fig. 7b together with the $B_x(x, y, I)$ data cube (Fig. 7a).

It shows that the symmetry of the hysteretic behavior remains with a decreasing magnitude versus the distance from the write pole down to 0 T as the sampling position goes out beyond 400 nm. A similar surface plot can be extracted to evidence how focused the magnetic induction is 5 nm in front of the writer, which is approximately the distance between the read/write head and the media in normal operation and is reported in Fig. 7c (extracted from position noted (2) on the Fig. 7a).

Further manipulations of the $B_x$ and $B_y$ data cubes allow quantifying the magnetic flux spreading by calculating $\tan^{-1}
\left| \frac{B_y}{B_x} \right|$ for a given current. It results in an image that exhibits the magnetic induction spread from the write pole source to the vacuum. In Fig. 8a is reported the angular spread of the magnetic flux observed for a +60 mA applied current. A quantitative measurement of the magnetic flux divergence can be extracted at the position where the magnetic media is flying 5 nm in front of the pole. For +60 mA applied current the

**Figure 7** a) The experimental $B_x(x, y, I)$ data cube of the write pole contribution, b) $B_x(I)$ surface plot of the hysteresis loops extracted from a) at $y = 0$ for increasing distance from the write pole (plane (1) in Fig 7a), c) $B_x(I)$ surface plot of the hysteresis loops extracted from a) as function of the lateral “$y$” positions and at a distance $x = 5$ nm from the pole (plane (2) in Fig 7a).
magnetic flux spreading over $\Delta \theta = 10^\circ$ angle (noted +/- 5° on Fig. 8b is radiating over a 15 nm wide region at 5 nm from the pole. We plot in Fig. 8a the variation of the radiated regions located at 5 nm in front of the pole as a function of the applied current and for various flux divergences. This demonstrates how the lateral shields are efficient in focusing the field onto the media for current varying between 10 mA and 60 mA and how the flux drops off laterally (to prevent interference across adjacent recorded tracks in the media). From the HDD application point of view this illustrates that only the media directly under the write pole will experience any significant magnetic interaction for writing/erasure processes.

4. Conclusions

In summary we have developed a new in situ TEM process allowing the quantitative measurement of the magnetic field generated by a HDD writer in operation at the nanometer scale. The combination of off-axis electron holography with micromagnetic simulations allows us to quantify the full magnetic response of the write pole to various applied currents. We demonstrate that there is no remnant field along the perpendicular direction to the surface of the write pole when no current is applied. We have been able to confidently determine the magnetic field in saturation conditions and to measure the local hysteresis loop for any point of the studied region. We show how to separate the different contributions of the shield and the write pole and characterize the angular spread of the magnetic field as a function of current. We have therefore demonstrated the power of holography to characterize active magnetic systems and provided baseline device characterization important for design of next generation write poles. As the control circuitry of the writer are designed to accommodate time varying signals up to the GHz range, further in situ electron holography experiments are now feasible to analyze the magnetic induction damping as function of the applied current frequency used in data storage.

In addition, this work has laid the foundation for the development of a new type of in situ magnetic instrumentation for TEM. A HDD write device could well be used to create a local magnetic source for fundamental magnetic studies in situ in TEM. Since the magnetic field coming off the pole tip is located in the in-plane direction, various magnetic nanomaterials could be placed into a tunable magnetic field generated by the write pole and their local magnetic response studied in situ. This would open up new methods for studying systems like data storage media under realistic conditions. Additionally, more exotic systems can now be explored in more detail such as magnetic nanoparticles, magnetic tunnel junctions or artificial spin ices [16,17].
Acknowledgements

The authors acknowledge the European Union under the Seventh Framework Programme under a contract for an Integrated Infrastructure Initiative Reference 312483-ESTEEM2 and the French National Research Agency under the “Investissement d’Avenir” program reference No. ANR-10-EQPX-38-01”. This work is supported by the French national project EMMA (ANR12 BS10 013 01).

Electronic Supplementary Material: Supplementary material giving some details about the sample preparation, the electron holography quantification and the micromagnetic simulation is available in the online version of this article at http://dx.doi.org/10.1007/s12274-****.****. (automatically inserted by the publisher).

References

Electronic Supplementary Material

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Supporting information to DOI 10.1007/s12274-****-****-* (automatically inserted by the publisher)

1. Sample preparation

The slider was firstly mechanical polished down to 30 µm along the z direction (see Fig. S1) using a tripod polishing system. The remaining bar of the slider containing the writing head as well as the contact pads was then mounted on a traditional TEM sample grid (insulating) laying along the (x,y) plane, contacts at the top (see Fig. S2.c). The device was then put into the FIB for growing two small carbon pillars (2µm wide, 5 µm long) by Ion Beam Induced Deposition on both sides (y direction) of the write pole (5 µm away on each side - see Fig. S2.a and b). The device was then mounted into a home-made sample holder allowing 2 vacuum feedthroughs towards the outside (Fig. S2.c). Wedge bonding was then use to connect the contact pads of the slider toward the dedicated contacts of the sample holder (Fig. S2.c enlargement).

![Figure S1 Cross-section SEM image of the read/write head. The magnetic shields and the write pole are evidenced. The yellow arrow indicates the flying direction of the magnetic media and the electron path for TEM experiments. This sectional view corresponds to the xz plane; the studied area is the xy plane.](image-url)
Figure S2

a) Carbon nanopillars deposited by FIBID allowing the location of the write pole for the TEM experiment.
b) TEM image of the write pole with the carbon pillars. The red square and the dashed line represent respectively the studied area in front of the write pole and the position of the biprism.
c) Image of the thin device positioned in the biasing stage with the wire bounding.

2. Electron holography

The phase shift of an electron beam that has interacted with an electromagnetic field is sensitive both to the electrostatic potential “$V$” and to the components of the magnetic vector potential “$A_z$” and integrated along the beam path.

The measured phase shift is derived from the Aharonov-Bohm expression giving the phase shift of a charged particles interacting with an electrostatic potentials and a magnetic vector potential [S1].

$$\phi(r) = C_E \int V(r, z) dz - \frac{e}{\hbar} \int A_z(r, z) dz$$ \hspace{1cm} (S1)

$$\phi(r) = C_E \int V(r, z) dz - \frac{e}{\hbar} \int B_z(r, z) dr \, dz$$ \hspace{1cm} (S2)

where \( C_E = \frac{2\pi}{\lambda} \frac{E_k + E_0}{E_k (E_k + 2E_0)} \)
• \( z \) is the direction of the incident beam,
• \( r \) is the position vector in the plane perpendicular to beam direction,
• \( A_z \) the component of the magnetic vector potential “\( A \)” along the beam direction,
• \( B_{\perp} \) the component of the magnetic induction perpendicular to both \( r \) and \( z \),
• \( V \) the electrostatic potential
• \( \lambda \) the electron wavelength
• \( E_0 \) the rest mass energy of the electrons
• \( E_k \) the kinetic energy of the electrons

In the vacuum and without the presence of any electrostatic field, which is the case in our study on the write head, only the second term of Eq. S2 is acting \([S2]\).

The phase image is calculated from the electron hologram performing its Fourier Transform (FT) and selecting one of the two side band reflections. The selecting reflection is masked and re-centered before to compute the Inverse Fourier Transform (FT\(^{-1}\)). This leads to a complex image whose amplitude image and phase image can be separated.

The resulting phase image is then
\[
\phi(r) = -\frac{e}{\hbar} \int B_{\perp}(r, z) dr dz \quad (S3)
\]
where \( r = (x, y) \) represents the position vector in the plane perpendicular to the electron path (\( x \) and \( y \) directions), \( e \) the elementary charge, \( B_{\perp} \) the component of the magnetic induction in the plane perpendicular to \( r \) and to the beam direction \( z \). The measured phase shift corresponds to a projection and an integration of all in-plane magnetic field contributions along the electron path. Numerical simulation are generally unavoidable to take into account the two dimensional projection of a three dimensional field. It then gives an image of the magnetic induction flux perpendicular to the electron beam direction and projected over the beam path. An image of the projected components \( B_x(r) = B_x(x, y) \) and \( B_y(r) = B_y(x, y) \) of the magnetic induction can be calculated performing a partial derivative of \( \phi(r) \) over \( y \) and \( x \) respectively

\[
\int B_x(r) dz = -\frac{\hbar}{e} \frac{d}{dy} \phi(r) \quad (S4)
\]
\[
\int B_y(r) dz = \frac{\hbar}{e} \frac{d}{dx} \phi(r)
\]

3. Micromagnetic and phase shift simulations

Micromagnetic simulations are performed using the finite element package Magpar \([S3]\) to simulate the entire write pole system using the dimensions of the write pole extracted from SEM images. We use the standard bulk values of the magnetic constants of the various materials comprising the write pole system (writer, shields, etc.) and generate the magnetic flux spreading in a tri-dimensional (1 µm, 1.5 µm, 0.8 µm) box in front of the whole device for an applied current of +40 mA (Fig. S3).

The resulting magnetic induction flux is used to calculate the phase shift of the electron beam passing across
the box by integrating the simulated $B_x(x,y)$ and $B_y(x,y)$, over the thickness of the box and following Eq. S3.

Figure S3 Box of (1.5 µm, 1 µm, 0.8 µm) used for the micromagnetic simulations. The write pole is located at position (0, 0, 0).

References